

# Photometric Calibration

The process of converting instrumental magnitudes to calibrated apparent magnitudes in a standard system is generally referred to as ‘photometric calibration’. The level of complexity at which this is done is dependent to a great extent on the quality of data which one has. If, for example, one has calibration data of milli-magnitude precision, it is necessary to worry about second order effects (such as the colour-term dependence of airmass corrections). This handout presumes data of somewhat more typical (i.e. poorer) quality, sufficient for calibrations with a precision of  $\sim 0.05$  mag. This level of uncertainty is typical of the that found in faint-object observations at modern CCD-equipped observatories.

Presume, for the moment, that one has observations of a number of fields in two filters (call these filters  $i$  and  $j$ ). The basic equation governing the apparent magnitude for a single object in the  $i$  filter is as follows:

$$m_i = m_{Ii} + A_{0i} + A_{1i} \times (\text{Airmass}) + A_{2ji} \times (m_j - m_i)$$

where

- $m_i, m_j$  are the magnitudes of the object in the standard system in the filters  $i$  and  $j$ ,
- $m_{Ii}$  is the instrumental magnitude of the object in filter  $i$ ,
- $A_{0i}$  is the zero-point in filter  $i$ ,
- $A_{1i}$  is the extinction coefficient in filter  $i$ , and
- $A_{2ji}$  is the colour term transformation coefficient in filter  $i$ , referenced to the  $j-i$  colour.

A similar equation governs filter  $j$ . Note that to compute the desired quantities ( $m_i$  and  $m_j$ ) one must establish the values of  $A_{0i}$ ,  $A_{1i}$  and  $A_{2ji}$ . This is the primary goal of the photometric calibration.

By observing standard stars, one knows in advance the values of  $m_i$ ,  $m_j$ , and can hence (with enough standard star observations) compute  $A_{0i}$ ,  $A_{1i}$  and  $A_{2ji}$ . Even with observations in only a single filter, one can compute the colour term coefficient  $A_{2ji}$ , as  $m_i$  and  $m_j$  are known a priori from the standard magnitude list. However, the *application* of this coefficient to the computation of the calibrated magnitude of unknown objects is not possible without some estimate of the intrinsic colour of said objects. It is hence usually not a useful exercise to compute a colour term coefficient for single filter observations, though some estimate of this may be useful in interpreting measurements of standard stars made in even a single filter.

In essence, provided that one has observations in filter  $i$  of standard stars of various colours, at various airmasses, it should be possible to compute  $A_{0i}$ ,  $A_{1i}$  and  $A_{2ji}$  for that filter. In practice, it may turn out that neither  $A_{1i}$  or  $A_{2ji}$  can be computed with any reliability, as the atmosphere may not be stable enough ( $A_{1i}$ ) or the colour range spanned by the standards not large enough ( $A_{2ji}$ ) to provide any useful information. At a good transparent site, the magnitude of  $A_{1i}$  should typically range from a few tenths to a few hundredths of a mag ( $U$  to  $I$  bands respectively), and  $A_{1i}$  should always be negative. The value of  $A_{2ji}$  depends on how closely the transmission of the site + telescope + filter + camera setup used to make the observations matches the standard filter curve used to define the standard system.